

# Collider Physics at NLO and the Monte Carlo MCFM

John Campbell  
*Argonne National Laboratory*

# *Outline*

- Introduction to Next-to-Leading-Order QCD
- Status of NLO: where we are now
- Why is NLO so difficult?
- Glimpses of the future: new directions for NLO calculations
- Introduction to MCFM
- MCFM at work:  $W + 2$  jet production
- Summary

# What is NLO?

In the context of this talk, I will use NLO to mean:

- $\mathcal{O}(\alpha_s)$  corrections to tree-level processes
  - graphs involving *one* virtual loop
  - no resummation of logarithms
  - no power corrections
  - no matching with parton showers
- When discussing NLO programs, they **will not be** event generators
  - predictions are parton level only, with no showering, hadronization or detector effects
  - for processes involving jets, one jet will contain at most two partons
- I will focus on high-energy colliders, in particular hadron colliders such as the Tevatron and the LHC

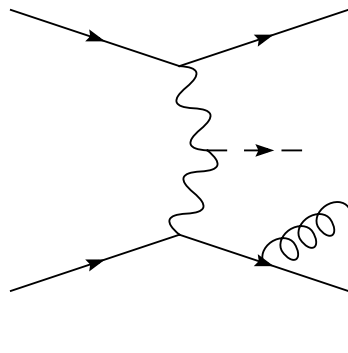
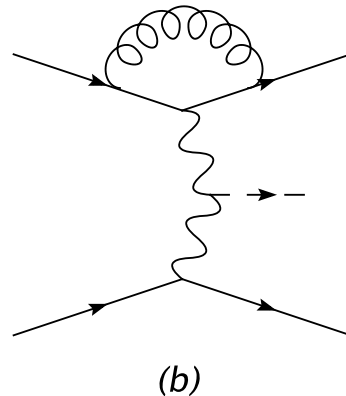
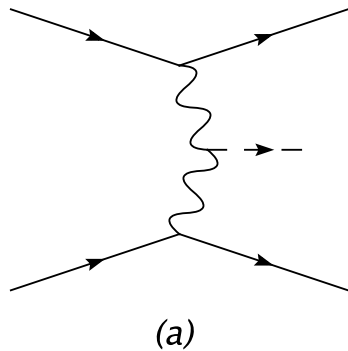
# *Why NLO?*

The benefits of higher order calculations are well known

- Less sensitivity to unphysical input scales
  - first predictive normalization of observables at NLO
  - more accurate estimates of backgrounds for new physics searches and (hopefully) interpretation
  - confidence that cross-sections are under control for precision measurements
- More physics
  - jet merging
  - initial state radiation
  - more parton fluxes
- It represents the first step for a plethora of other techniques
  - matching with resummed calculations
  - NLO parton showers

# NLO diagrams

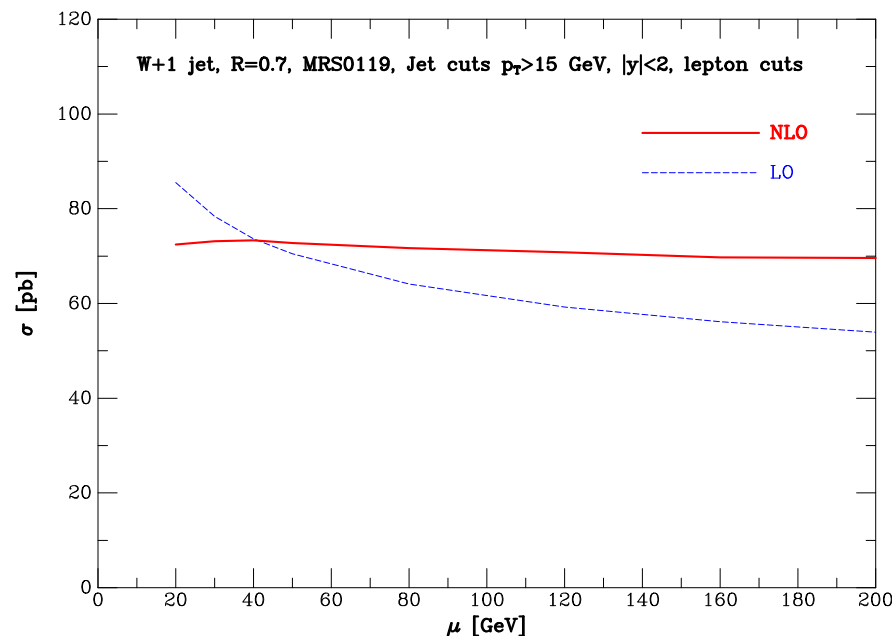
■ Vector-boson fusion at a hadron-hadron collider:  $pp \longrightarrow H + 2 \text{ jets}$



- (a) Lowest order
- (b) NLO: virtual
- (c) NLO: real

# Scale dependence

- $W + 1$  jet cross-section demonstrates the reduced scale dependence that is expected at NLO, as large logarithms are partially cancelled.

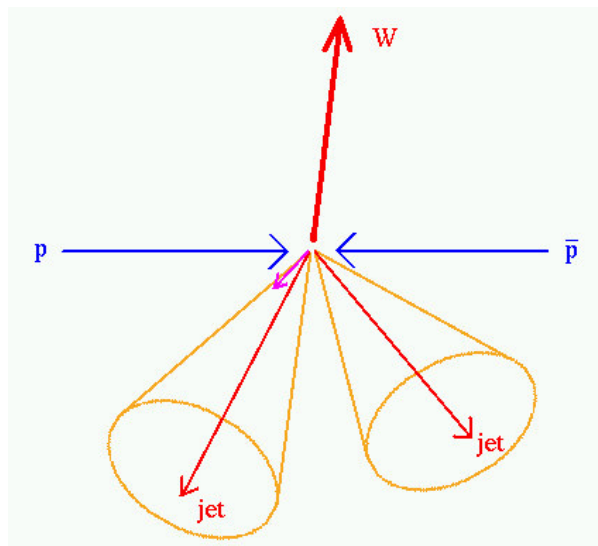


- Change between low  $\sim 20$  GeV and high  $\sim 80$  GeV scales is about 30% at LO and  $< 5\%$  at NLO.

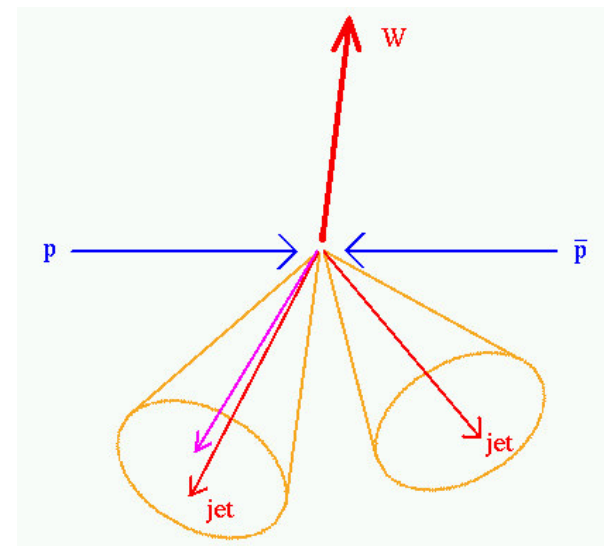
# Next-to-leading order

- At next-to-leading order, we include an extra “unresolved” parton in the final state

soft



collinear



- The theory begins to look more like an experimental jet, so one expects a better agreement with data.

# So ....

If all this is true then, given that we have invested heavily (both financially and intellectually) in new upgrades and colliders like Run II of the Tevatron and the LHC:

- What's the current state-of-the-art?
  - NLO tools currently available
- Why are we lacking NLO predictions for many interesting (and crucial) processes?
  - traditional methods
  - difficulties and hurdles
- What's being done about it?
  - promising new directions



# An experimenter's wishlist

■ Hadron collider cross-sections one would like to know at NLO

Run II Monte Carlo Workshop, April 2001

Single boson	Diboson	Triboson	Heavy flavour
$W + \leq 5j$	$WW + \leq 5j$	$WWW + \leq 3j$	$t\bar{t} + \leq 3j$
$W + b\bar{b} + \leq 3j$	$WW + b\bar{b} + \leq 3j$	$WWW + b\bar{b} + \leq 3j$	$t\bar{t} + \gamma + \leq 2j$
$W + c\bar{c} + \leq 3j$	$WW + c\bar{c} + \leq 3j$	$WWW + \gamma\gamma + \leq 3j$	$t\bar{t} + W + \leq 2j$
$Z + \leq 5j$	$ZZ + \leq 5j$	$Z\gamma\gamma + \leq 3j$	$t\bar{t} + Z + \leq 2j$
$Z + b\bar{b} + \leq 3j$	$ZZ + b\bar{b} + \leq 3j$	$WZZ + \leq 3j$	$t\bar{t} + H + \leq 2j$
$Z + c\bar{c} + \leq 3j$	$ZZ + c\bar{c} + \leq 3j$	$ZZZ + \leq 3j$	$t\bar{b} + \leq 2j$
$\gamma + \leq 5j$	$\gamma\gamma + \leq 5j$		$b\bar{b} + \leq 3j$
$\gamma + b\bar{b} + \leq 3j$	$\gamma\gamma + b\bar{b} + \leq 3j$		
$\gamma + c\bar{c} + \leq 3j$	$\gamma\gamma + c\bar{c} + \leq 3j$		
	$WZ + \leq 5j$		
	$WZ + b\bar{b} + \leq 3j$		
	$WZ + c\bar{c} + \leq 3j$		
	$W\gamma + \leq 3j$		
	$Z\gamma + \leq 3j$		

# NLOJET++

Author(s): Z. Nagy

<http://www.ippp.dur.ac.uk/~nagyz/nlo++.html>

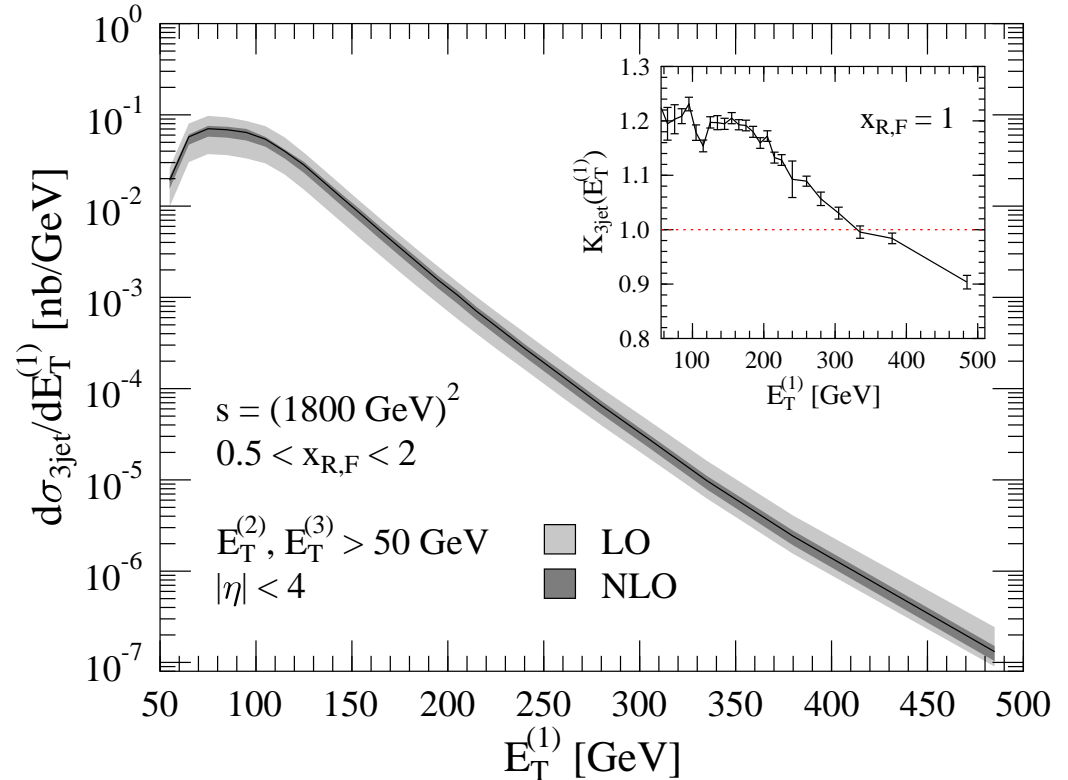
Multi-purpose C++ library for calculating jet cross-sections in  $e^+e^-$  annihilation, DIS and hadron-hadron collisions.

$k_\perp$  algorithm

$e^+e^- \longrightarrow \leq 4 \text{ jets}$

$ep \longrightarrow (\leq 3 + 1) \text{ jets}$

$p\bar{p} \longrightarrow \leq 3 \text{ jets}$



hep-ph/0110315

# AYLEN/EMILIA

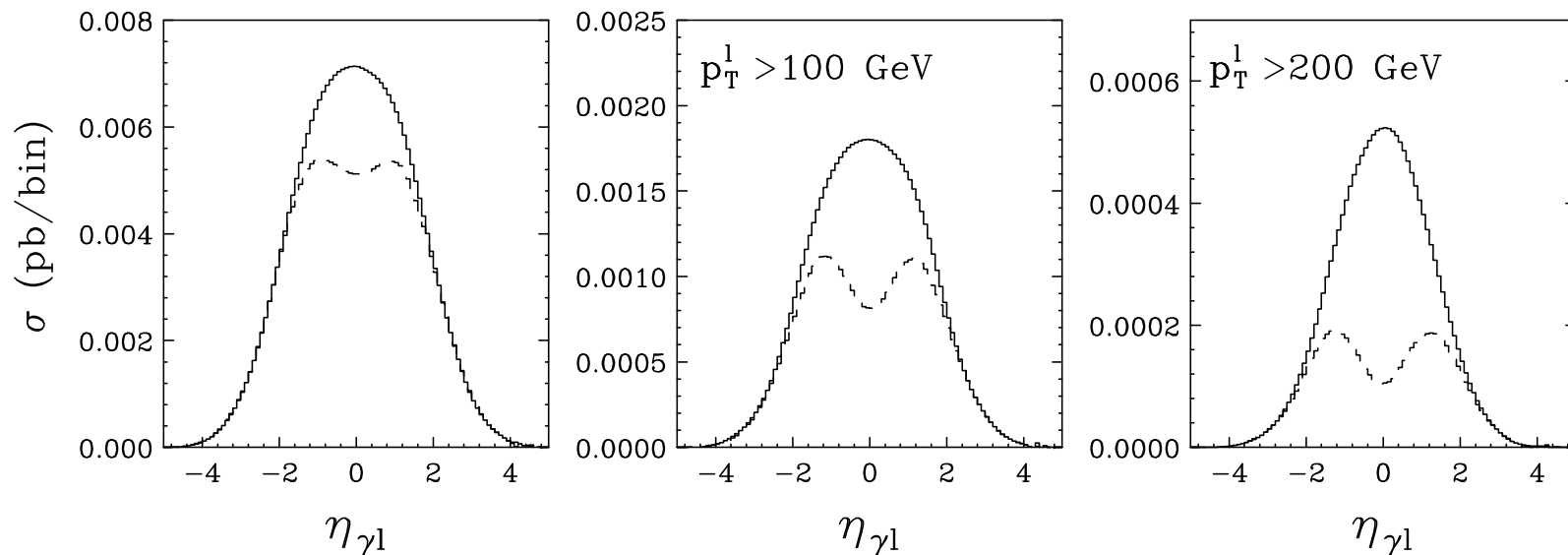
Author(s): L. Dixon, Z. Kunszt, A. Signer, D. de Florian

<http://www.itp.phys.ethz.ch/staff/dflorian/codes.html>

Fortran implementation of gauge boson pair production at hadron colliders, including full spin and decay angle correlations.

$$p\bar{p} \longrightarrow VV' \quad \text{and} \quad p\bar{p} \longrightarrow V\gamma \quad \text{with } V, V' = W, Z$$

Anomalous triple gauge boson couplings at the LHC:



hep-ph/0002138

# MCFM

Author(s): JC, R. K. Ellis

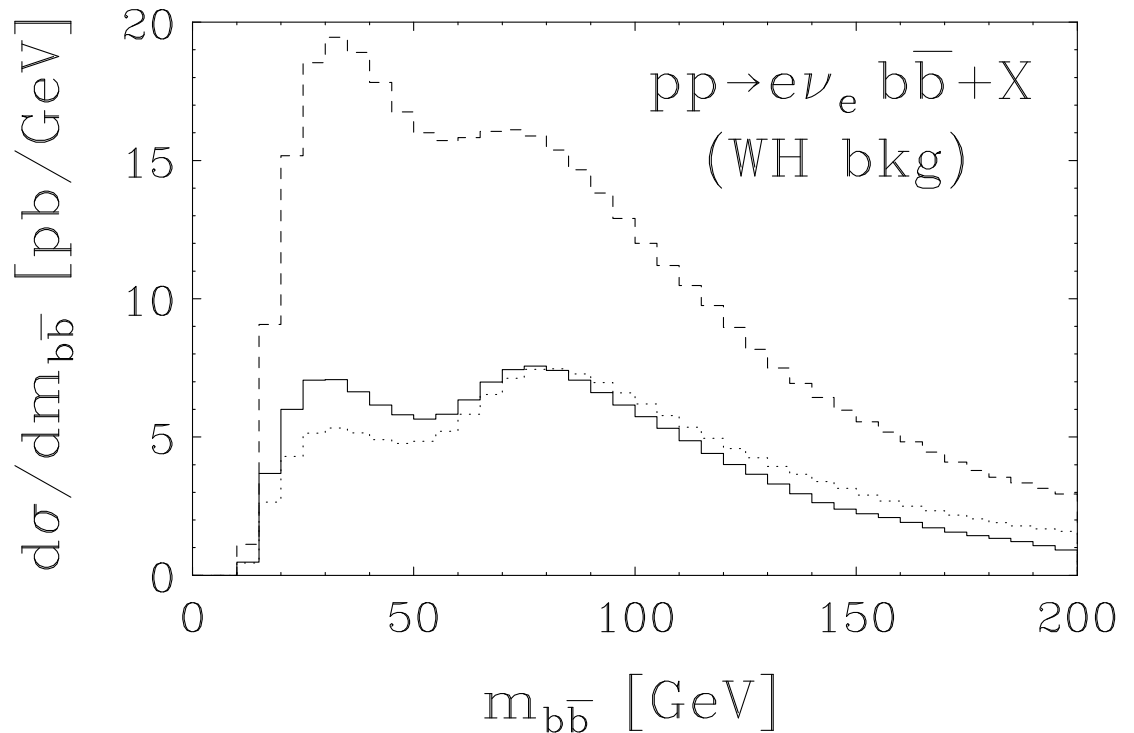
<http://mcfm.fnal.gov>

Fortran package for calculating a number of processes involving vector bosons, Higgs, jets and heavy quarks at hadron colliders.

$$p\bar{p} \longrightarrow V + \leq 2 \text{ jets}$$

$$p\bar{p} \longrightarrow V + b\bar{b}$$

with  $V = W, Z$ .



hep-ph/0308195

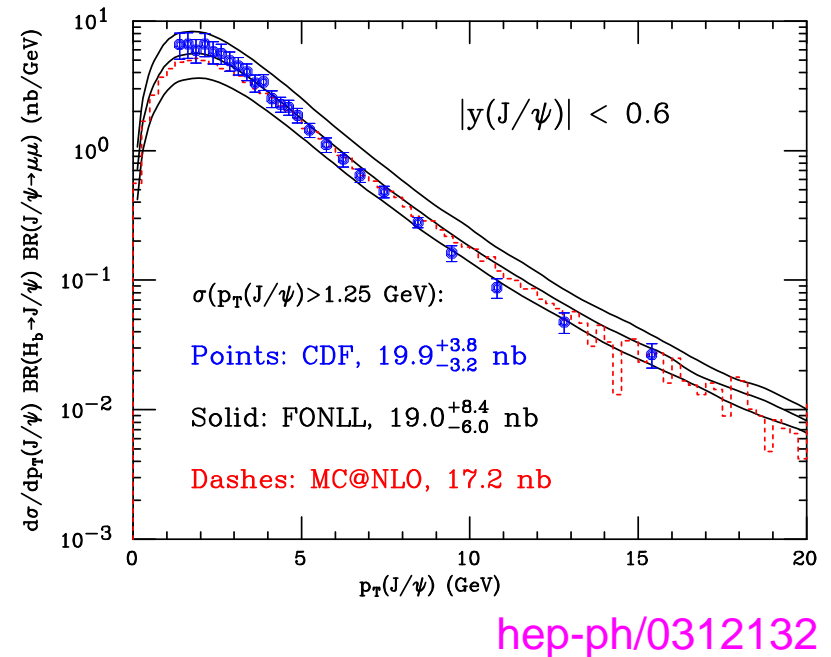
# Heavy quark production

Author(s): M. L. Mangano, P. Nason and G. Ridolfi

<http://www.ge.infn.it/~ridolfi/hvqlibx.tgz>

Fortran code for the calculation of heavy quark cross-sections and distributions in a fully differential manner

- Based on the more inclusive calculations of Dawson et al, Beenakker et al.
- Does not include multiple gluon radiation,  $\log(p_T/m_b)$  (FONLL)  
Cacciari et al., hep-ph/9803400
- These are the same matrix elements that are incorporated into MC@NLO  
Frixione et al., hep-ph/0305252

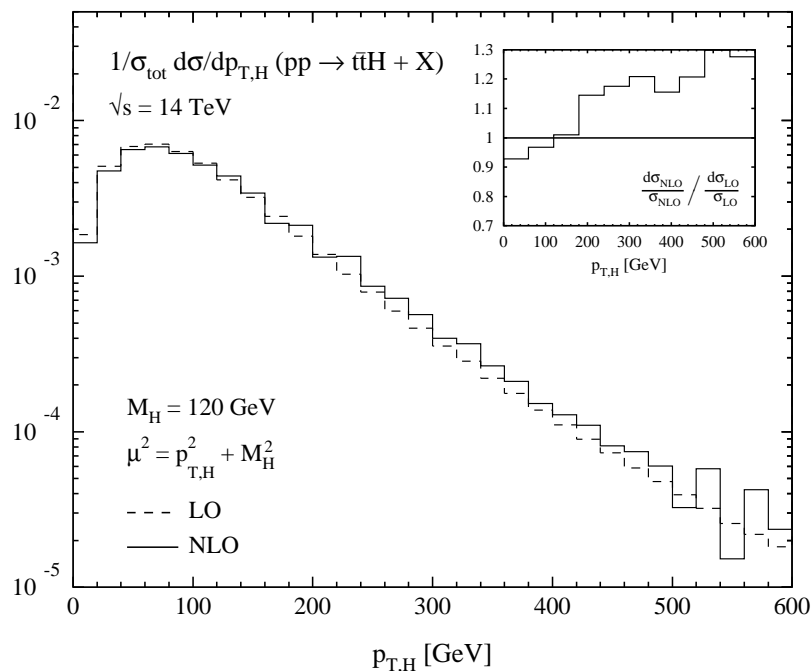


# Higgs + $Q\bar{Q}$

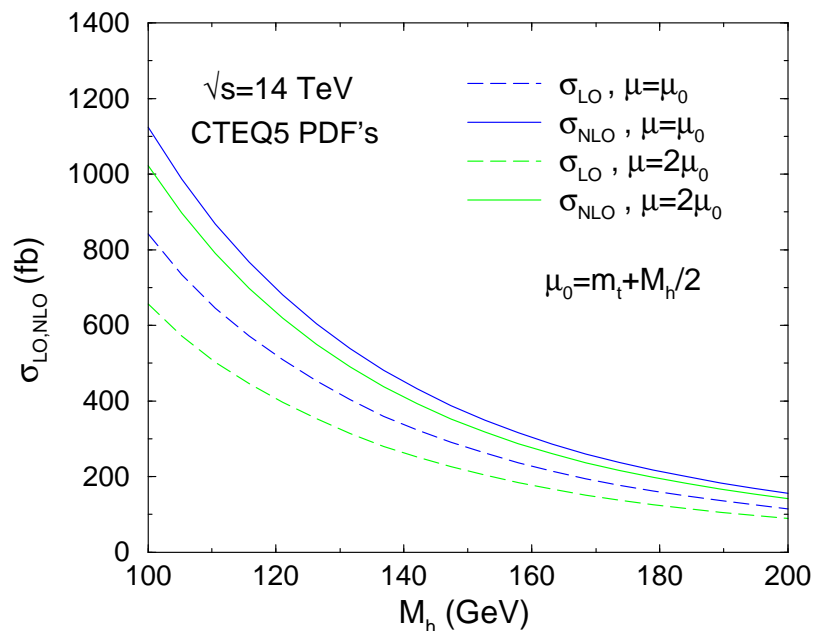
Author(s): S. Dawson, C. B. Jackson, L. H. Orr, L. Reina, D. Wackeroth;  
W. Beenakker, S. Dittmaier, M. Kramer, B. Plumper, M. Spira, P. Zerwas  
(No public code released)

Associated production of a Higgs and a pair of heavy quarks,

$$p\bar{p} \longrightarrow Q\bar{Q}H, \quad \text{with } Q = t, b.$$



hep-ph/0211352



hep-ph/0311216

# Theoretical status

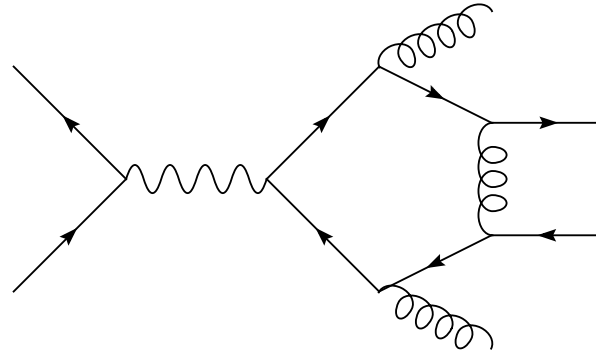
■ Much smaller jet multiplicities, some categories untouched

Single boson	Diboson	Triboson	Heavy flavour
$W + \leq 2j$	$WW + \leq 0j$	$WWW + \leq 3j$	$t\bar{t} + \leq 0j$
$W + b\bar{b} + \leq 0j$	$WW + b\bar{b} + \leq 3j$	$WWW + b\bar{b} + \leq 3j$	$t\bar{t} + \gamma + \leq 2j$
$W + c\bar{c} + \leq 0j$	$WW + c\bar{c} + \leq 3j$	$WWW + \gamma\gamma + \leq 3j$	$t\bar{t} + W + \leq 2j$
$Z + \leq 2j$	$ZZ + \leq 0j$	$Z\gamma\gamma + \leq 3j$	$t\bar{t} + Z + \leq 2j$
$Z + b\bar{b} + \leq 0j$	$ZZ + b\bar{b} + \leq 3j$	$WZZ + \leq 3j$	$t\bar{t} + H + \leq 0j$
$Z + c\bar{c} + \leq 0j$	$ZZ + c\bar{c} + \leq 3j$	$ZZZ + \leq 3j$	$t\bar{b} + \leq 0j$
$\gamma + \leq 1j$	$\gamma\gamma + \leq 1j$		$b\bar{b} + \leq 0j$
$\gamma + b\bar{b} + \leq 3j$	$\gamma\gamma + b\bar{b} + \leq 3j$		
$\gamma + c\bar{c} + \leq 3j$	$\gamma\gamma + c\bar{c} + \leq 3j$		
	$WZ + \leq 0j$		
	$WZ + b\bar{b} + \leq 3j$		
	$WZ + c\bar{c} + \leq 3j$		
	$W\gamma + \leq 0j$		
	$Z\gamma + \leq 0j$		

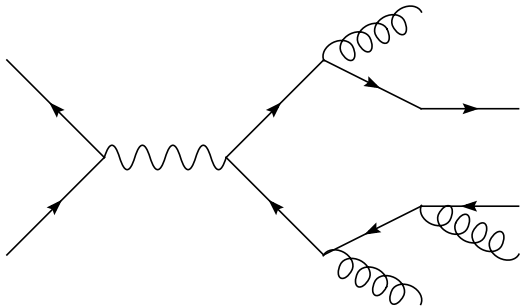
# NLO basics

VIRTUAL

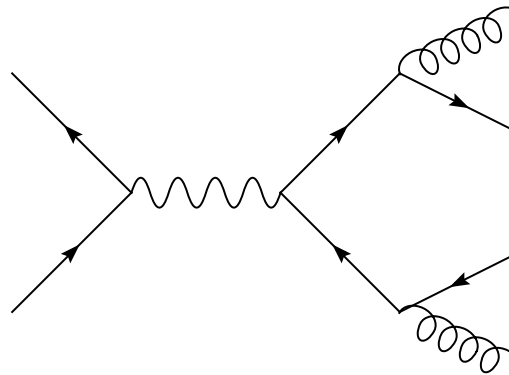
$$\int d^{4-2\epsilon}\ell \ 2\mathcal{M}_{loop}^* \mathcal{M}_{tree} \\ = \left(\frac{A}{\epsilon^2} + \frac{B}{\epsilon}\right) |\mathcal{M}_{tree}|^2$$



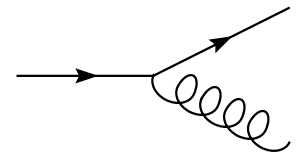
REAL



$$|\mathcal{M}_{tree+1}|^2$$



$$|\mathcal{M}_{tree}|^2$$



$$\int (Split) dPS \\ = - \left(\frac{A}{\epsilon^2} + \frac{B}{\epsilon}\right)$$



# Slow progress

- Why has progress been so slow?

$$e^+e^- \longrightarrow 3 \text{ jets} \quad \text{c. 1980}$$

R. K. Ellis et al., 1981

$$e^+e^- \longrightarrow 4 \text{ jets} \quad \text{c. 2000}$$

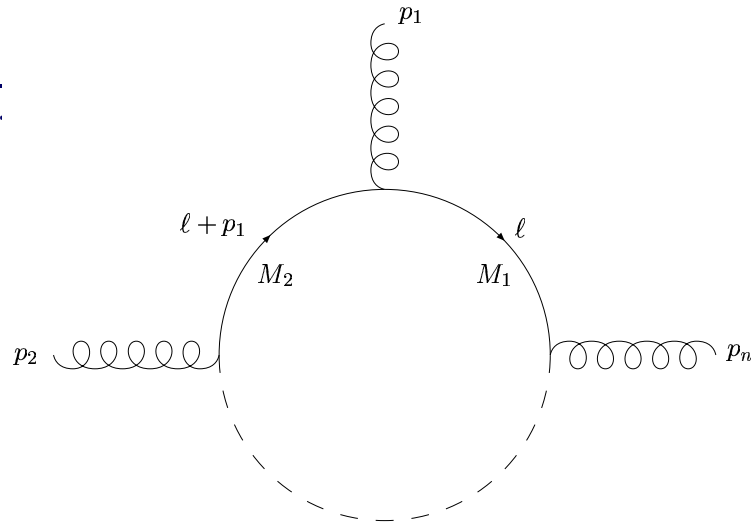
Bern et al., Glover et al., 1996-7

- More particles  $\rightarrow$  many scales  $\rightarrow$  lengthy analytic expressions
- Integrals are complicated and process-specific:

$$\int d^{4-2\epsilon} \ell \frac{1}{(\ell^2 - M_1^2)((\ell + p_1)^2 - M_2^2)}.$$

- different for:

$$\begin{array}{ll} p_i^2 \neq 0 & W, Z, H \\ M_i^2 \neq 0 & t, b, \dots \end{array}$$



# Complications

- Fermions and non-Abelian couplings lead to more complicated tensor integrals:

$$\int d^{4-2\epsilon} \ell \frac{\ell^\mu}{(\ell^2 - M_1^2)((\ell + p_1)^2 - M_2^2) \dots}$$

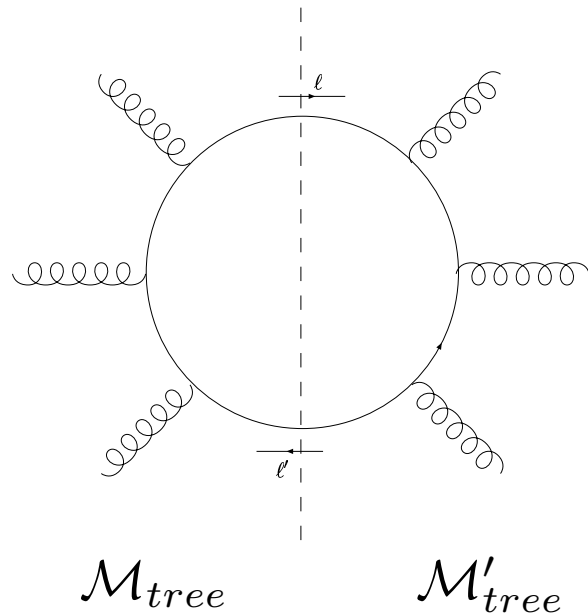
- Passarino-Veltman reduction in terms of scalar integrals:

$$\longrightarrow c_1 p_1^\mu + \dots c_{n-1} p_{n-1}^\mu$$

where the  $c_i$  are given by the solutions of  $(n - 1)$  equations

- This gives rise to the  $(n - 1) \times (n - 1)$  Gram determinant,  $\Delta = \det(2p_i \cdot p_j)$ .
  - large intermediate expressions
  - spurious singularities

# Unitarity technique



$$= \int dPS(\ell, \ell') \mathcal{M}_{tree} \times \mathcal{M}'_{tree}$$

- Standard tree-level tricks can be used to simplify amplitudes, yielding compact results  
e.g. Dixon, hep-ph/9601359
- Rational functions of invariants cannot be obtained easily with this method
- Not easy to generalize and automate, simplification by hand

# Hexagons and beyond

- There is little computational experience with  $N$ -point integrals beyond pentagons,  $N = 5$  : the NLO frontier is at  $2 \rightarrow 3$  processes
- However, we know that all integrals with  $N > 4$  can be written as a sum of known box integrals

Binoth et al., hep-ph/9911342

- Analytic result is:

$$N - \text{point finite part} = \sum^m \text{dilogarithms} + \text{simpler functions}$$

- For a hexagon integral with masses,  $m > 1000$ . This may lead to large cancellations in some kinematic regions and thus numerical instabilities
- Perhaps a numerical method could be just as good, or better

Binoth et al., hep-ph/0210023

Ferrogia et al., hep-ph/0209219

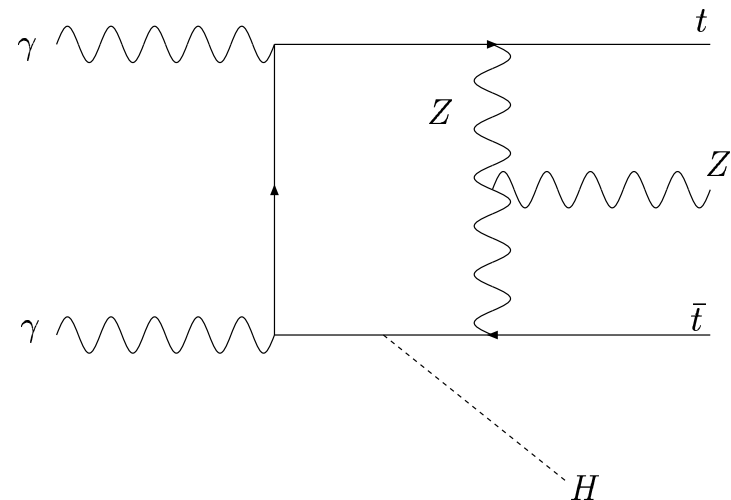
# Numerical recipe

The diagram illustrates the hexagon reduction formula. On the left is a red hexagon labeled  $D = 4$ . This is followed by an equals sign. To the right of the equals sign is a summation symbol with a '20' above it, followed by a red triangle labeled  $D = 4$ . This is followed by a plus sign, then another summation symbol with a '15' above it, followed by a red square labeled  $D = 6$ .

$$\text{Hexagon } (D=4) = \sum_{20} \text{Triangle } (D=4) + \sum_{15} \text{Box } (D=6)$$

Hexagon reduction in terms of triangles and boxes

- A **sector decomposition** is used to simplify the integrals
- triangles  $\longrightarrow$  1-dim. integral
- boxes  $\longrightarrow$  2-dim. integral
- Integration by a combination of standard techniques and Monte Carlo



# *IR-divergent loop integrals*

- The IR singularities can be isolated from the loop integrals using a simple technique

Dittmaier, hep-ph/0308246

- Singularities occur when:
  - a massless external particle splits into two massless internal lines

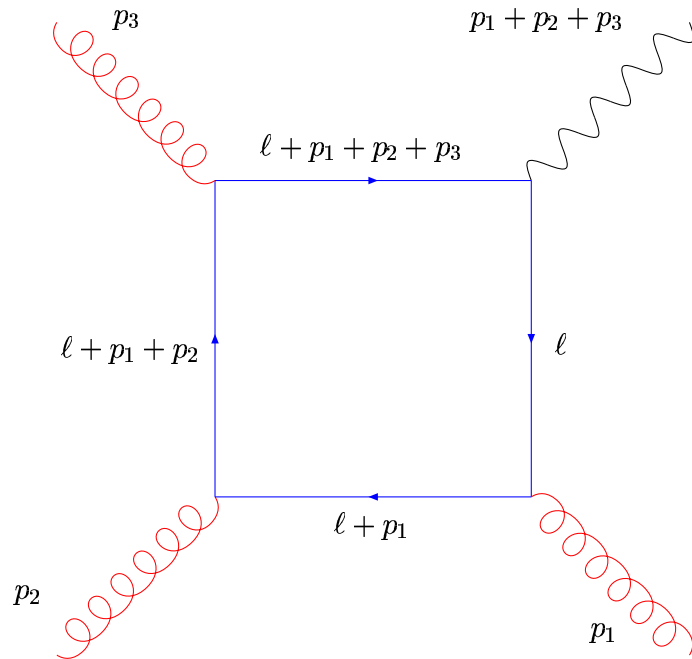
COLLINEAR

two external on-shell particles exchange a massless particle

SOFT

- These result in  $\frac{1}{\epsilon}$ ,  $\frac{1}{\epsilon^2}$  poles
- By identifying all the soft and collinear configurations in an integral, one can extract all the IR poles and obtain a finite integral that can be evaluated in 4 dimensions.
- Singular pieces are given in terms of related triangle integrals

# Example



$$p_1^2 = p_2^2 = p_3^2 = 0$$

$\ell = -p_1 - p_2$   
yields **soft** singularities

$\ell = xp_1$  for any arbitrary  $x$   
leads to **collinear** singularities

$$\frac{1}{(\ell + p_1 + p_2)^2 (\ell + p_1 + p_2 + p_3)^2} \longrightarrow \frac{A}{(\ell + p_1 + p_2)^2} + \frac{B}{(\ell + p_1 + p_2 + p_3)^2}$$

- This method has already been applied to pentagon integrals involved in the calculation of  $t\bar{t}H$  production at NLO

# *Numerical approach*

- If all singularities can be subtracted, perhaps loop integrals can be done numerically
- This method has many advantages:
  - a general solution for many processes, regardless of internal and external masses
  - extension to large final-state multiplicities limited only by CPU power
  - presence of masses in general should simplify the procedure (less singularities) rather than requiring much more work (cf. analytical approach)
- Problem: loop integrals also contain UV divergences

$$\int d^{4-2\epsilon} \ell \frac{\ell^\mu \ell^\nu}{\ell^2 (\ell + p_1)^2 (\ell + p_1 + p_2)^2}$$



# *UV singularities*

- Problem of UV subtraction solved and outlined by Nagy and Soper  
Nagy and Soper, hep-ph/0308127

- At the moment, limited to QCD with  $m_Q = 0$

- Schematically,

$$\sum \underbrace{(\text{Graph} - \text{CT})}_{\text{finite}} + \underbrace{\left( \sum \text{CT} \right)}_{\text{simple}}$$

where CT stands for the sum of UV, soft and collinear counter-terms

- Loop integration can then be performed numerically
- General algorithm laid out, but the details of the numerical integration provide a topic for further study

see also e.g. Soper, hep-ph/9804454

- Recent alternative proposed, isolating all IR and UV singularities  
Giele and Glover, hep-ph/0402152

# *Real contribution*

- Relatively simple - diagrams and phase space can already be generated efficiently by tree level programs
- Methods for dealing with singular regions are well-developed, such as [phase-space slicing](#) and [dipole subtraction](#)
- However, for high multiplicity final states, the number of singular regions is large, resulting in:
  - Very many dipoles
  - Time-consuming calculation of subtraction terms
- Modifications to the original formalism have been made that limit the subtraction region and thus speed up the code
- There's room for investigation of this implementation and further ideas

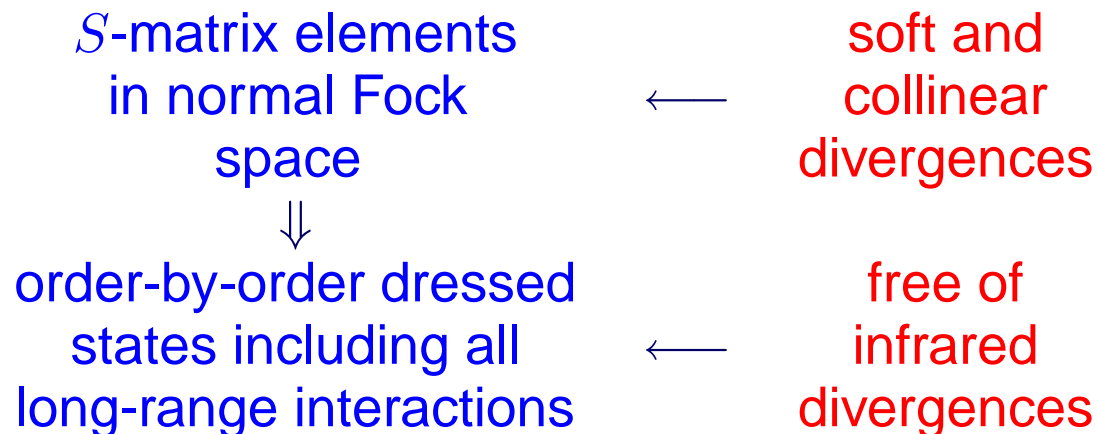
Z. Nagy, [hep-ph/0307268](#)

# *A different approach*

- Try to construct infrared finite amplitudes for gauge theories with massless fermions

Forde and Signer, hep-ph/0311059

- Finite amplitudes would have many benefits:
  - Simple numerical approach
  - Easy matching to a parton shower



# Basic idea

- Basic assumption when constructing amplitudes normally:

$$\underbrace{e^{-itH}}_{\text{full Hamiltonian}} \underbrace{|\Psi(t)\rangle}_{\text{exact state}} \longrightarrow \underbrace{e^{-itH_0}}_{\text{free Hamiltonian}} \underbrace{|\Phi(t)\rangle}_{\text{free state}} \quad \text{as } t \rightarrow \pm\infty$$

- This assumption is not true for QCD: massless gauge bosons have long-range interactions that do not vanish sufficiently quickly  $\longrightarrow$  IR singularities
- Introduce an asymptotic Hamiltonian that contains the long-range interactions that give rise to soft and collinear splittings:

$$e^{-itH_A} |\Omega(t)\rangle$$

- Diagrammatic rules similar to Feynman rules, but time-ordered
- So far, only demonstrated on a test case ( $e^+e^- \rightarrow 2$  jets): no hadronic initial state, no triple-gluon coupling

# *NLO Summary*

- NLO tools are an invaluable aid to experimental studies now and will continue to be so in the future
- There are many programs currently available for predictions at both existing and proposed colliders
  - author-controlled  
single top,  $H + Q\bar{Q}$
  - single class of processes  
 $V\gamma, Q\bar{Q}$
  - generic programs  
NLOJET++, PHOX-family, MCFM
- Despite recent progress towards NNLO predictions, there's still much left to be done at the one-loop level

# *NLO at Present*

- Although there are now new methods being proposed for performing NLO (and beyond) calculations, the ideas are so far embryonic
- No method has yet been implemented in a practical form. Although the promise is great, for producing NLO predictions involving multi-particle final states, these methods still struggle to reproduce known results of 20 years ago
- Emerging data from the Tevatron Run II and studies for the LHC require NLO results now
- Thus there is still much effort devoted towards traditional calculations. One such implementation is the general purpose Monte Carlo **MCFM**

JC and R. K. Ellis

# MCFM Summary - v. 3.4

$$p\bar{p} \rightarrow W^\pm / Z$$

$$p\bar{p} \rightarrow W^\pm + Z$$

$$p\bar{p} \rightarrow W^\pm + \gamma$$

$$p\bar{p} \rightarrow W^\pm + g^* (\rightarrow b\bar{b})$$

$$p\bar{p} \rightarrow W^\pm / Z + 1 \text{ jet}$$

$$p\bar{p}(gg) \rightarrow H$$

$$p\bar{p}(VV) \rightarrow H + 2 \text{ jets}$$

$$p\bar{p} \rightarrow W^+ + W^-$$

$$p\bar{p} \rightarrow Z + Z$$

$$p\bar{p} \rightarrow W^\pm / Z + H$$

$$p\bar{p} \rightarrow Z b\bar{b}$$

$$p\bar{p} \rightarrow W^\pm / Z + 2 \text{ jets}$$

$$p\bar{p}(gg) \rightarrow H + 1 \text{ jet}$$

- MCFM aims to provide a unified description of a number of hadron-hadron processes at **NLO** accuracy. More processes are available at LO only.
- Various leptonic and/or hadronic decays of vector bosons are included as further sub-processes.
- MCFM version 3.4.5 is part of the CDF code repository.

# *MCFM Information*

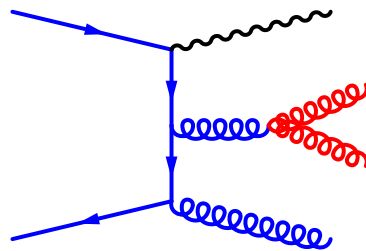
- Version 3.4 available at:  
<http://mcfm.fnal.gov>
- Improvements over previous releases:
  - more processes
  - better user interface
  - support for PDFLIB, Les Houches PDF accord  
(→ PDF uncertainties)
  - ntuples as well as histograms
  - unweighted events
  - Pythia/Les Houches generator interface (LO)
  - 'Behind-the-scenes' efficiency
- Coming attractions:
  - even more processes
  - photon fragmentation



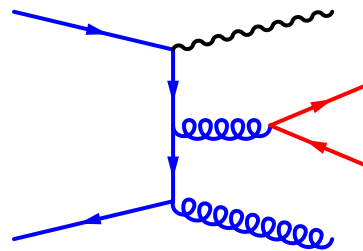
# *Example: $W + 2 \text{ jet production at NLO}$*

- Feynman diagrams for extra parton radiation, e.g.

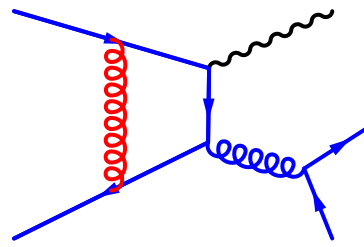
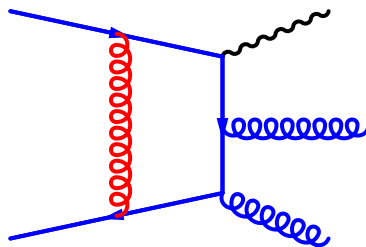
soft gluon



collinear quarks

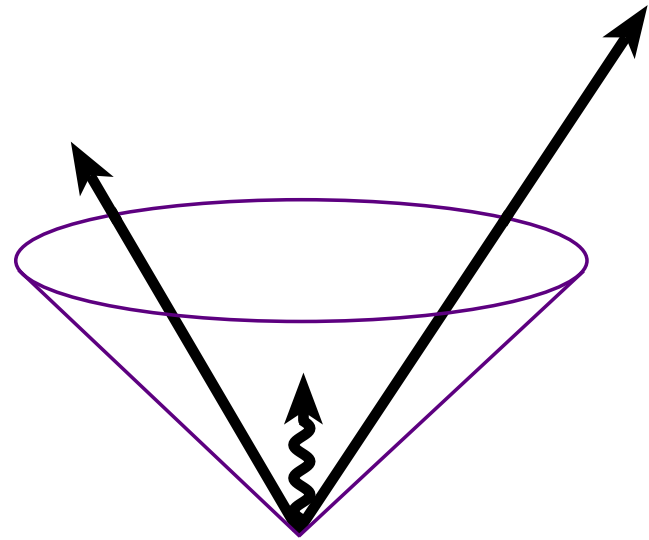
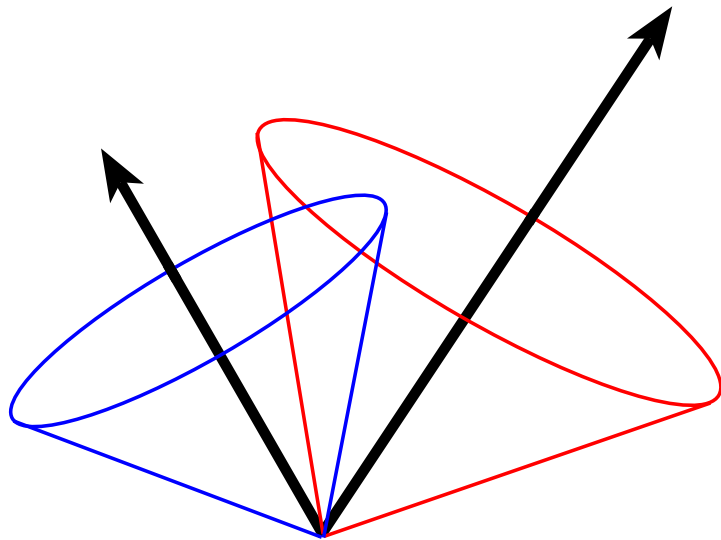


- Loop diagrams, also one extra factor of  $\alpha_S$ :



# Defining a jet - cone algorithm

- Cone-based algorithm,  $\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2} > R$ .
- Very popular in Run I.
- Suffers from sensitivity to soft radiation at NLO.



- Instability can be mitigated by extra jet seeds, e.g. midpoint algorithms.

# *Defining a jet - $k_T$ algorithm*

- Preferred by theory - insensitive to soft radiation, immediate matching to resummed calculations.
- Limited experimental use at hadron colliders due to difficulties with energy subtraction.
- Jets are clustered according to the relative transverse momentum of one jet with respect to another.
- Similarity with cone jets is kept, since the algorithm still terminates with all jets having  $\Delta R > R$ .
- We shall adopt the  $k_T$  prescription that is laid out for Run II (G. Blazey et al.), where other ambiguities such as the jet recombination scheme are fixed.

# *Tevatron event cuts*

- $k_T$  clustering algorithm with pseudo-cone size,  $R = 0.7$ .

- Jet cuts:

$$p_T^{\text{jet}} > 15 \text{ GeV}, |y^{\text{jet}}| < 2.$$

- Lepton cuts:

$$p_T^{\text{lepton}} > 20 \text{ GeV}, |y^{\text{lepton}}| < 1.$$

- (W only) Missing transverse momentum:

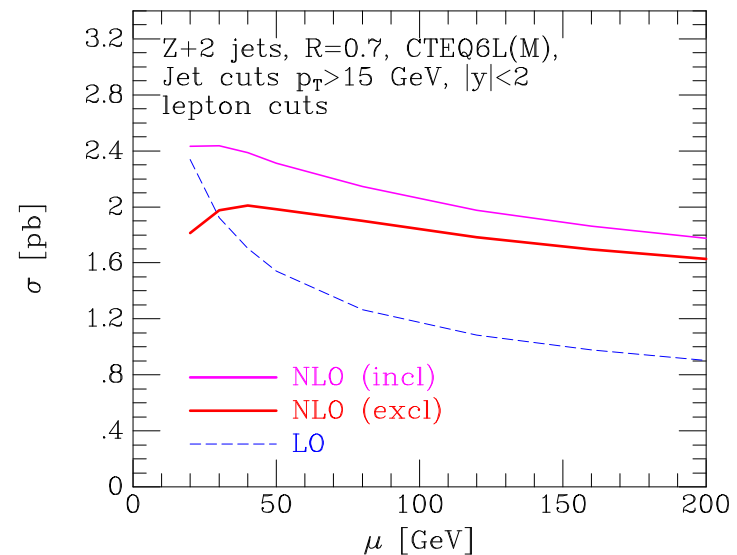
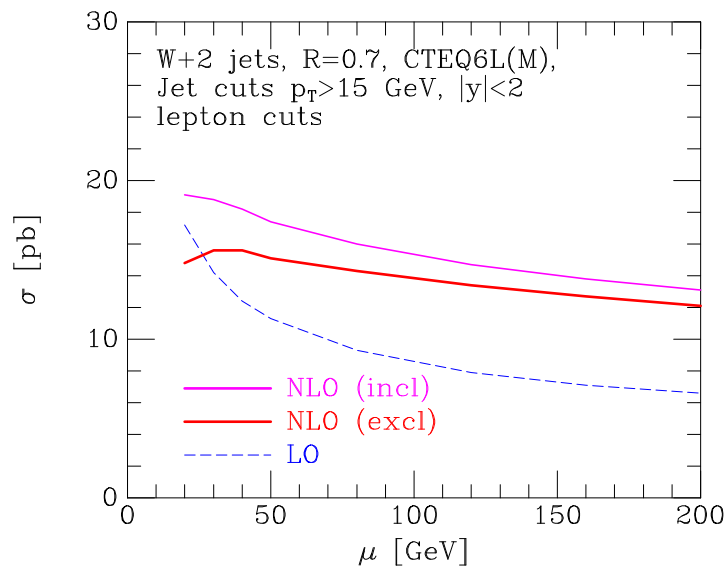
$$p_T^{\text{miss}} > 20 \text{ GeV}.$$

- (Z only) Dilepton mass:

$$m_{e^-e^+} > 15 \text{ GeV} \text{ (since } \gamma^* \text{ is also included)}.$$

# Scale dependence

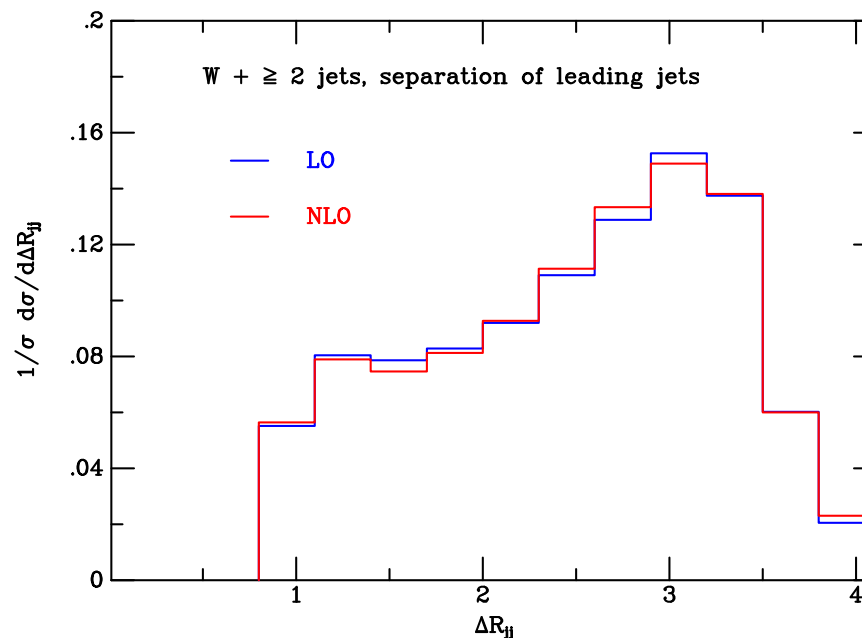
- Choose equal factorization and renormalization scales and examine the scale dependence of the  $W, Z + 2$  jets cross-section at the Tevatron, in LO and NLO.



- Exclusive cross-section requires exactly 2 jets at NLO. Inclusive also includes the (lowest order) 3 jet contribution.
- Scale dependence is much reduced in both cases.

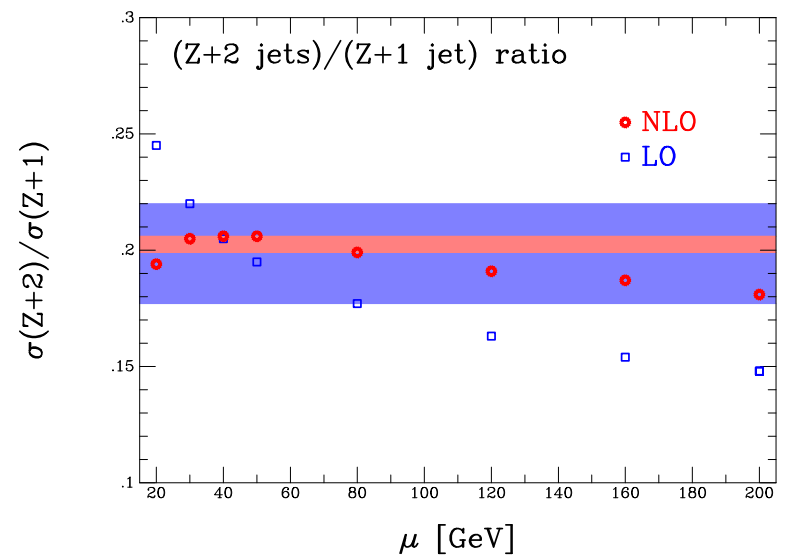
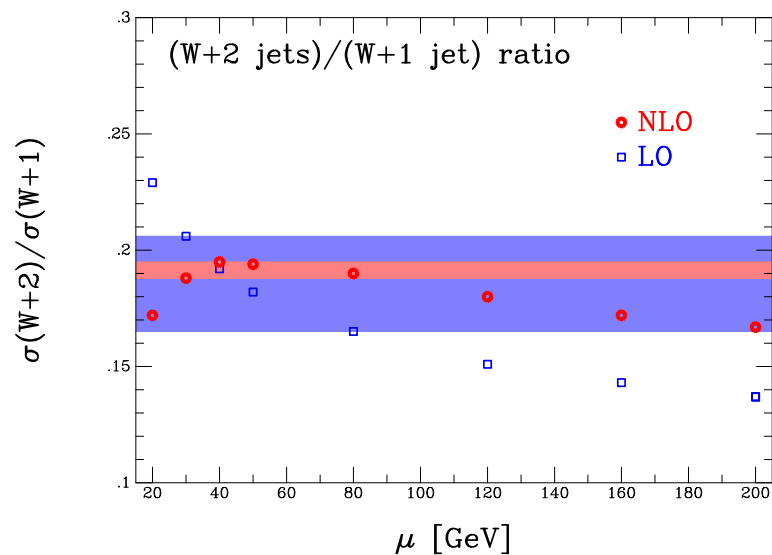
# Jet-jet separation

- In Run I, there was some discrepancy in the shape of the jet-jet separation  $\Delta R_{jj}$  compared with LO theory.
- Results at NLO appear to confirm the leading order shape, with no significant dependence on scale.



# Cross-section ratios at NLO

- Prediction for the (W+2 jet)/(W+1 jet) ratio in Run II. Preferred experimentally since some systematics cancel.



- As expected, much more stable at NLO than LO, particularly in the region of conventional scales  $\sim 30 - 80$  GeV.
- More studies underway.

# Heavy flavour content

- Many signals of new physics involve the production of a  $W$  or  $Z$  boson in association with a heavy particle that predominantly decays into a  $b\bar{b}$  pair.

- Most well-known example is a light Higgs:

$$p\bar{p} \longrightarrow W(\rightarrow e\nu)H(\rightarrow b\bar{b})$$

$$p\bar{p} \longrightarrow Z(\rightarrow \nu\bar{\nu}, \ell\bar{\ell})H(\rightarrow b\bar{b})$$

- However, we will need to understand our SM backgrounds very well to perform this – or any similar – search.
- The largest background is ‘direct’ production:

$$p\bar{p} \longrightarrow W g^*(\rightarrow b\bar{b})$$

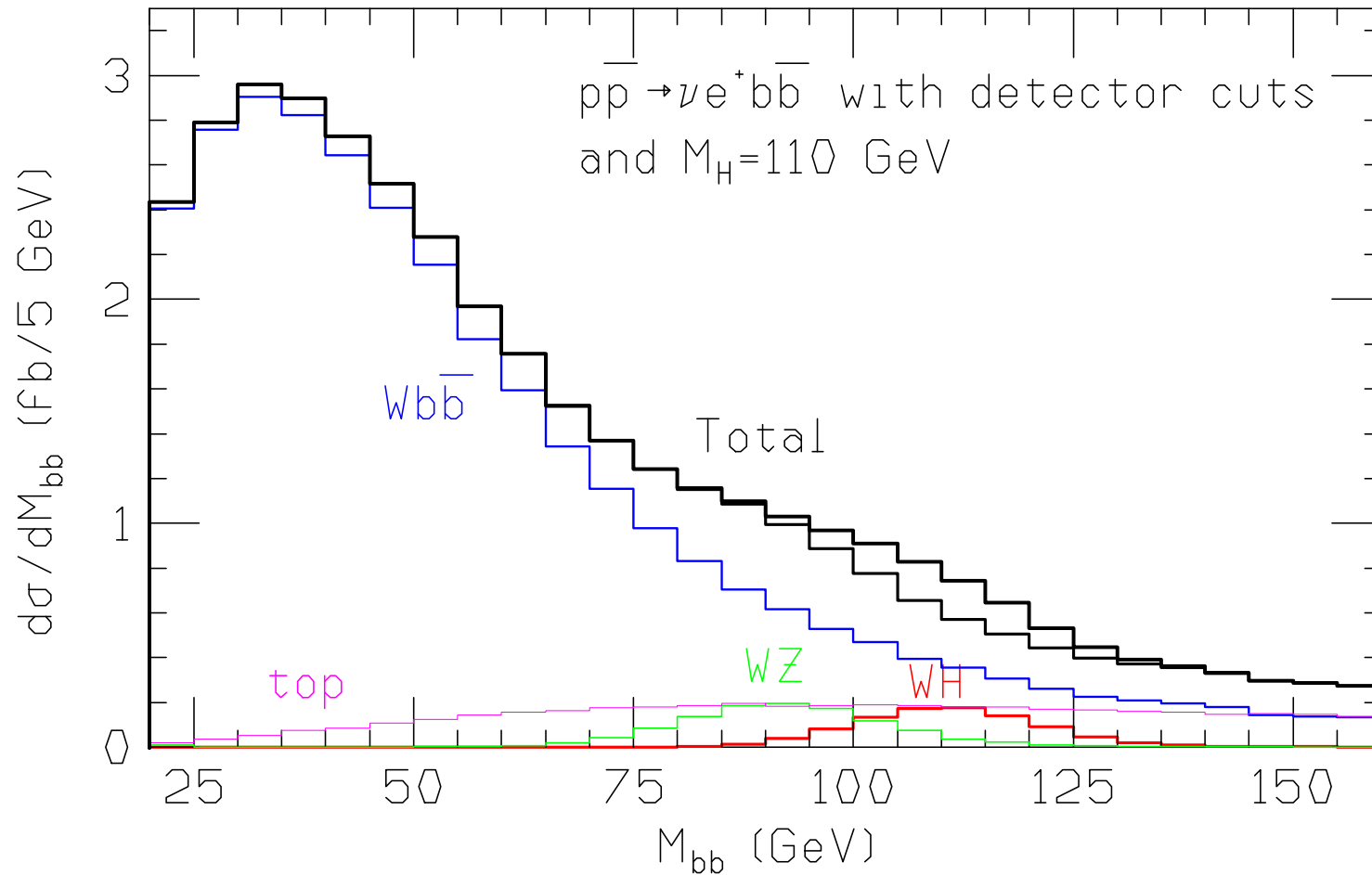
$$p\bar{p} \longrightarrow Z b\bar{b}$$

- Also important to understand these as backgrounds to signals that we expect, such as top.



# Background importance

- NLO study of  $WH$  search using MCFM.



# *Predicting the $Wb\bar{b}$ background*

- There are a number of methods for predicting the Standard Model ‘direct’ background.
- Amongst the theoretical choices are:
  - Fixed order vs. event generator;
  - LO vs. NLO;
  - Pythia vs. Herwig;
  - Massive  $b$ ’s vs. Massless  $b$ ’s.
- Citing a 40% uncertainty on the leading-order calculation (M. Mangano), a recent study by CDF uses a mixed approach relying heavily on generic  $W + \text{jet}$  data, but with some theoretical input.

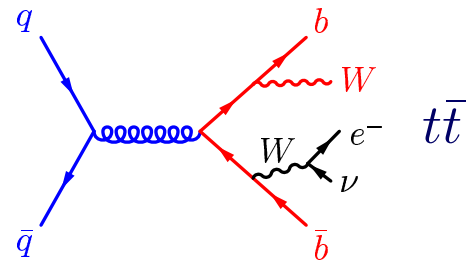
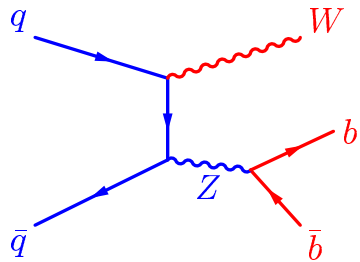
# Hybrid recipe (CDF's 'Method 2')

1. Measure the number of  $W + 2$  jet events.
2. Subtract the number of events predicted by theory from non-direct channels.
  - $t\bar{t}$  (Pythia norm. to NLO)
  - Diboson (Pythia norm. to NLO)
  - Single top (Pythia/Herwig norm. to NLO)
3. This estimates the number of direct  $W + 2$  jet events.
4. Use VECBOS (ALPGEN in Run II) (leading order) + Herwig to estimate the fraction of  $W + 2$  jet events that contain two  $b$ 's.
5. Obtain prediction for direct  $W + b\bar{b}$  events:

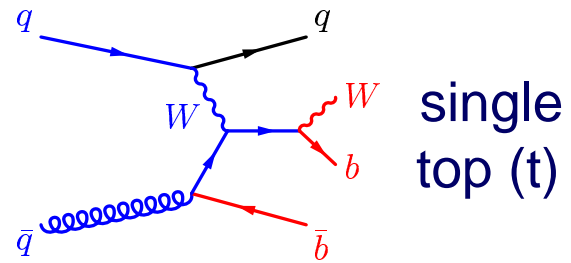
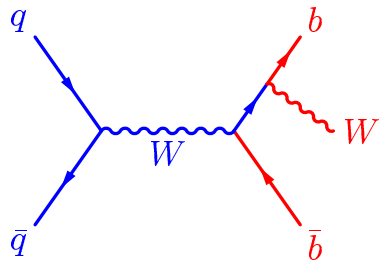
$$\sigma(Wb\bar{b}) = \left[ \frac{\sigma(Wb\bar{b})}{\sigma(W + 2 \text{ jet})} \right]_{MC} \times [\sigma(W + 2 \text{ jet})]_{\text{data}}$$

# Other $Wb\bar{b}$ backgrounds

diboson



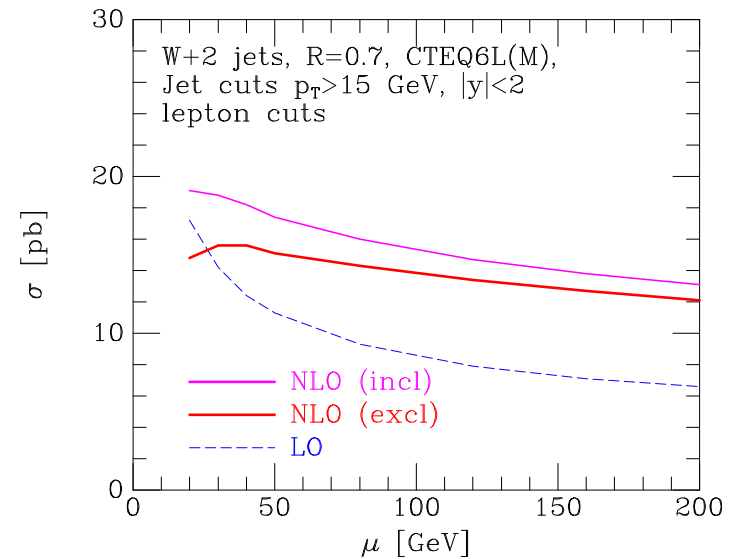
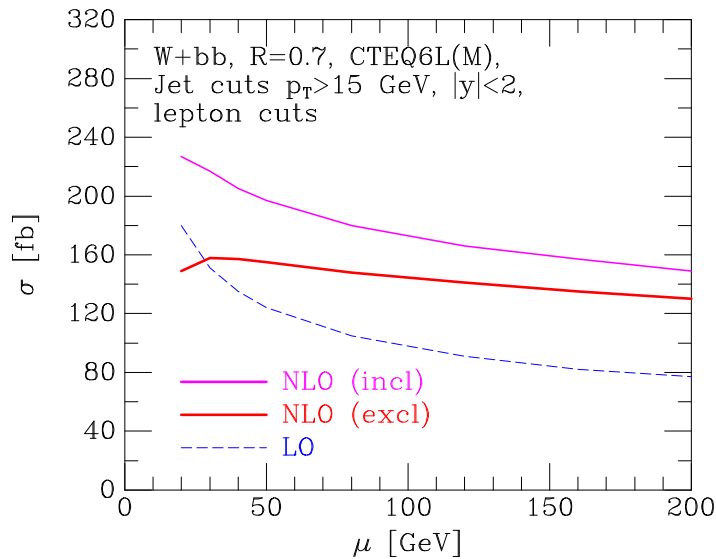
single  
top (s)



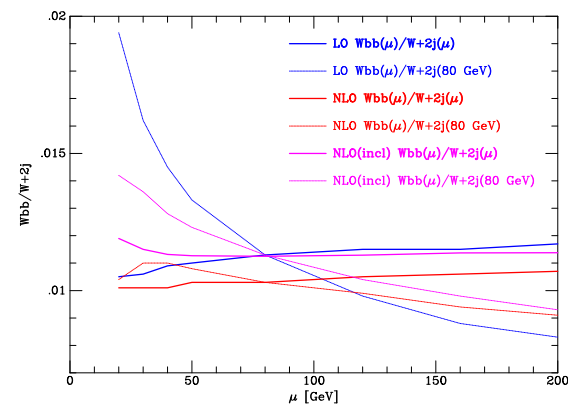
# *Alternatives - is this the best we can do?*

- VECBOS suffers from the same leading order uncertainty, albeit in a ratio now.
- We can calculate the  $Wb\bar{b}$  cross-section at NLO in MCFM. This has a much reduced scale dependence, but suffers from no showering and massless  $b$ 's.
- Another option is to calculate the same fraction that is calculated by LO+Herwig, but at NLO.
- One sees a much reduced scale dependence in each of the cross-sections at NLO, but ...
  - If we choose the same scales in the numerator and denominator, is the ratio also stable?
  - If the same scale is not appropriate, is this ratio useful?  $Wb\bar{b}$  is simply gluon-splitting at LO, suggesting a different renormalization scale may be appropriate.

# Scale dependence - $Wb\bar{b}$ vs. $W + 2 \text{ jets}$

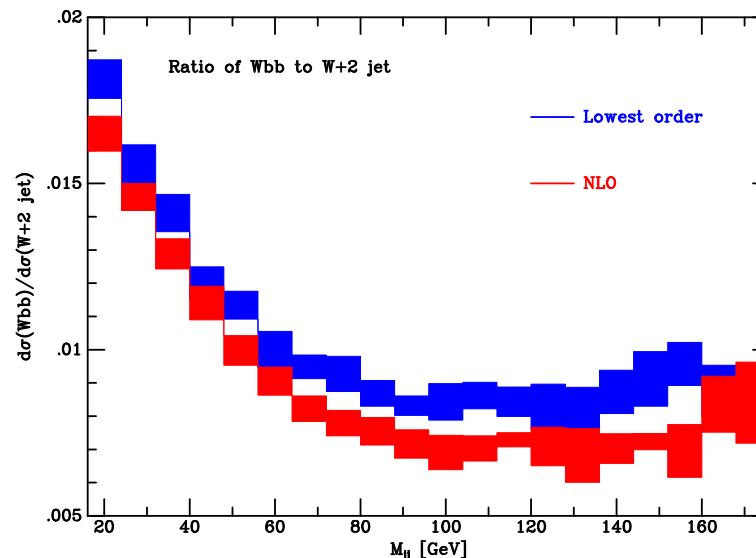


Ratio is much more stable at NLO,  
whether or not the same scale  
is used for  $Wb\bar{b}$  as for  $W + 2 \text{ jets}$ .



# Heavy flavour fraction vs. $m_{JJ}$

- Look at the variation of the ratio as the scale is changed (in both numerator and denominator) from  $\sim 30$  GeV up to  $\sim 160$  GeV.



- The ratio of  $b$ -tagged to untagged jets changes little at NLO and appears to be predicted reasonably well by perturbation theory.
- The fraction peaks at low  $M_{jj}$ , but in the reliable domain  $M_{jj} > 60$  GeV, the value is fairly constant  $\sim 0.8\%$ .

# Summary of MCFM

- MCFM is a state-of-the-art Monte Carlo for making NLO predictions at hadron colliders.
- The current version of the program is **MCFM v3.4**, which can be found at [mcfm.fnal.gov](http://mcfm.fnal.gov).
- This includes NLO corrections for  $W/Z + 2$  jets, which demonstrate the expected improvements such as a reduction in scale dependence. However, expectations for some observables are considerably changed at NLO.
- Implications of these calculations for the Tevatron are being studied. For instance, the fraction of a  $W + 2$  jet sample that contains two  $b$ -jets can be predicted at NLO and appears fairly robust
- There are many interesting studies to be done - from tests of QCD to backgrounds for new physics.

JC and Huston



# *Long-term outlook*

- It seems clear that performing NLO calculations on a case-by-case basis is not the way of the future
- An automated approach, combining algebraic and numerical recipes, appears both promising (in terms of physics output) and feasible
  - Extensions of existing algorithmic tree-level programs (such as ALPGEN and Madgraph/MadEvent) seem inevitable
- However, even if such ambitious projects can be realized, the story does not end there
  - interpretation and grooming of results will still be very process-specific
  - jet-clustering, photon fragmentation, threshold effects, resummation and more will need to be considered